

Measurement of Moment of Inertia by Retardation Test in Three-Phase Induction Motor

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Abstract— In this paper, an experiment is explained thoroughly which demonstrates the process of measuring the moment of inertia for three phase Induction Motor of 5 Hp. The rated speed of the Motor is 1440 rpm. The voltage and current ratings are 440 volts and 7 amps respectively. The method used to get the results is Retardation test. Multiple readings are taken for different values of speed, for calculation of moment of inertia of the machine. Using some standard formula, the final result is obtained. The test set up is set in the laboratory.

Keywords— *Electrical Machines AC, Induction Motor, Moment of Inertia, Retardation Test, Drives and Control.*

I. INTRODUCTION

The moment of inertia can be directly found out, when the mass of the different parts of load is known. If the mass of various parts of the load is unknown, then the Moment of Inertia can be obtained experimentally. The method is known as Retardation Test. In a Load-Motor System, it is very important to balance the motor and load torque. The motor torque is balanced by load torque and dynamic torque ($J \cdot d\omega_m/dt$). Retardation test is usually performed for DC-Motor Drives. But taking certain things into consideration, Retardation Test can also be performed in Induction motor successfully, yielding results good enough to get approximately original value of Moment of inertia.

II. CONCEPT

The moment of inertia is calculated by retardation test. The induction motor drive is run at rated speed. The the supply is cut off. The drive continues to run at rated speed at reted speed due to stored kinetic energy and decelerates due to rotational mechanical loses. The variation of speed with respect to time is noted. At ant speed ω_m , power P consumed in supplying rotational lossesis given by

$P = \text{Rate of change in kinetic Energy}$

$$\text{Or, } P = \frac{d}{dt} \left(\frac{1}{2} J \omega^2 \right) \dots\dots 1$$

$$\text{Or, } P = J \omega_m \frac{d\omega_m}{dt} \dots\dots\dots 2$$

From retardation test $\frac{d\omega_m}{dt}$, at rated, speed is obtained. The drive is then, reconnected with the supply and run at rated speed. The rotational mechanical power input to the drive is measured. This is approximately equal to P. now J can be measured from equation 2.

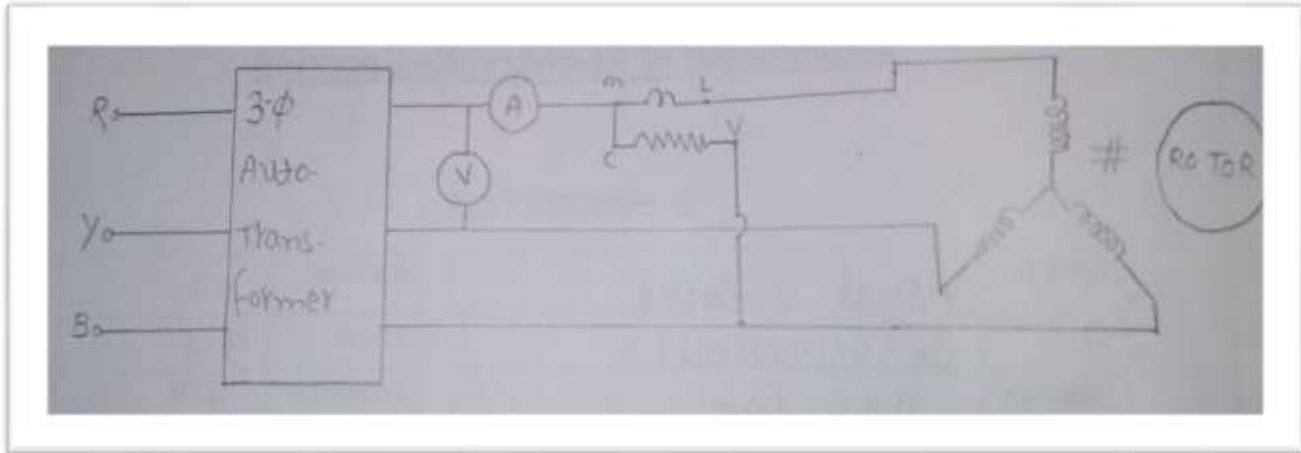


FIGURE 1: circuit diagram of retardation test

III. EQUIPMENT'S USED AND TEST SETUP

The following photograph shows the experiment set up in the laboratory. The photograph clearly shows the equipments required to perform the test.



FIGURE 2: Retardation test set up in laboratory for Experiment

3.1 INDUCTION MOTOR DRIVE

A 5 HP induction motor is used. The rated rpm of the motor is 1440. The motor is provided with 3 phase rated supply. The supply voltage has to be controlled at different stage. In order to get proper value we can use connection involving single phase also.

3.2 AUTOTRANSFORMER

The supply voltage has to be controlled at different stage. In order to get control the supply voltage autotransformer is used. It is very important for this experiment to run the machine at rated speed.

3.3 MEASURING DEVICES

Three measuring devices used for this experiment are Tachometer to measure speed, Wattmeter to measure power and voltmeter to measure the voltage. We need to record the time with reference to the fall in speed. Time is noted by using stop watch.



FIGURE 3: Measuring devices for experiment

IV. OBSERVATION TABLE AND CALCULATION

**TABLE 1
 OBSERVATION TABLE**

SL.NO	SPEED RPM	TIME SEC
1	1148	5
2	816	10
3	630	15
4	381	20
5	227	25

N= speed in RPM

$$W = \text{Angular velocity rad/sec} = \frac{2\pi N}{60}$$

$$P = \text{rate of change in kinetic energy} = J W m \frac{dW_m}{dt} = J \frac{2\pi N}{60} \frac{2\pi N}{60} \frac{dN}{dt}$$

$$\frac{dN_1}{dt} = \frac{816-630}{5} = 37.2$$

$$\frac{dN_2}{dt} = 49.8$$

$$\frac{dN_3}{dt} = 30.8$$

Average= 39.26

P= 160 watts (from measurement)

N= 1440 rpm (from measurement)

$$160 = 1.01 \times J \times 1440 \times 39.26$$

$$J = 0.257 \text{ kg/m}^3$$

V. CONCLUSION

In conclusion, we are successful in finding the value in moment of inertia for our induction motor drive, without physically weighing any part of the machine.

REFERENCES

- [1] G. Eason, B. Noble, and I. N. Sneddon, "On certain integrals of Lipschitz-Hankel type involving products of Bessel functions," *Phil. Trans. Roy. Soc. London*, vol. A247, pp. 529–551, April 1955.
- [2] J. Clerk Maxwell, *A Treatise on Electricity and Magnetism*, 3rd ed., vol. 2. Oxford: Clarendon, 1892, pp.68–73.
- [3] I. S. Jacobs and C. P. Bean, "Fine particles, thin films and exchange anisotropy," in *Magnetism*, vol. III, G. T. Rado and H. Suhl, Eds. New York: Academic, 1963, pp. 271–350.
- [4] K. Elissa, "Title of paper if known," unpublished.
- [5] R. Nicole, "Title of paper with only first word capitalized," *J. Name Stand. Abbrev.*, in press.
- [6] J. Morren, S.W.H. de Haan, W.L. Kling, J.A. Ferreira *Engineering IEEE Transactions on Power Systems* 2006 (First Published: 1 February 2006)
- [7] J. Groot, *State-of-Health Estimation of Li-ion Batteries: Cycle Life Test Methods*, Thesis for the degree of Licentiate of Engineering, Division of Electric Power Engineering, Department of Energy and Environment. Göteborg, Sweden, Chalmers University of Technology.
- [8] Y. B. Adyapaka Apatya, *Designing and Prototyping of 3-Phase Induction Motor*, "IEEE", 2017.
- [9] *Electric Motor Drives Modelling, Analysis and Control* –By R. Krishnan
- [10] *Dynamic Modeling of Induction Motor Using Rotor Rotating Reference Frame* Sonakshi Gupta, Dr. Sulochana Wadhvani PG Student [ISD], Dept. of EE, Madhav Institute of Technology & Science, Gwalior, M.P., India Associate Professor, Dept. of EE, Madhav Institute of Technology & Science, Gwalior, M.P., India.
- [11] P.C. and C. H. Thomas, "Simulation of Symmetrical Induction Machinery", *IEEE Transaction on Power Apparatus and Systems*, Vol. 84, November 1965, pp. 1038-1053.
- [12] C.Sankaran, *Power Quality*, CRC PRESS, 2002.